

$$1-12. \quad t_1 = \gamma \left( t_1' + \frac{vx_1'}{c^2} \right) \quad t_2 = \gamma \left( t_2' + \frac{vx_2'}{c^2} \right) \quad (\text{from Equation 1-21})$$

$$(a) \quad t_2 - t_1 = \gamma \left( t_2' + \frac{vx_2'}{c^2} - t_1' - \frac{vx_1'}{c^2} \right) = \gamma (t_2' - t_1')$$

(b) The quantities  $x_1'$  and  $x_2'$  in Equation 1-21 are each equal to  $x_o'$ , but  $x_1$  and  $x_2$  in Equation 1-20 are different and unknown.

$$1-13. \quad (a) \quad \gamma = 1/\sqrt{1-v^2/c^2} = 1/\sqrt{1-(0.85c)^2/c^2} = 1.898$$

$$x' = \gamma(x - vt) = 1.898[75\text{ m} - (0.85c)(2.0 \times 10^{-5}\text{ s})] = -9.537 \times 10^3\text{ m}$$

$$y' = y = 18\text{ m}$$

$$z' = z = 4.0\text{ m}$$

$$t' = \gamma(t - vx/c^2) = 1.898[2.0 \times 10^{-5}\text{ s} - (0.85c)(75\text{ m})/c^2] = 3.756 \times 10^{-5}\text{ s}$$

$$(b) \quad x = \gamma(x' + vt') = 1.898[-9.537 \times 10^3\text{ m} + (0.85c)(3.756 \times 10^{-5}\text{ s})] = 75.8\text{ m}$$

(difference is due to rounding of  $\gamma$ ,  $x'$ , and  $t'$ .)

$$y = y' = 18\text{ m}$$

$$z = z' = 4.0\text{ m}$$

$$t = \gamma(t' + vx'/c^2) = 1.898[3.756 \times 10^{-5}\text{ s} + (0.85c)(-9.537 \times 10^3\text{ m})/c^2] \\ = 2.0 \times 10^{-5}\text{ s}$$

1-14. To show that  $\Delta t = 0$  (refer to Figure 1-9 and Example 1-3).

$$t_1 = \frac{L}{\sqrt{c^2 - v^2}} + \frac{L}{\sqrt{c^2 - v^2}} = \frac{2L}{\sqrt{c^2 - v^2}} = \frac{2L}{c} \frac{1}{\sqrt{1 - v^2/c^2}}$$

$t_2$ , because length parallel to motion is shortened, is given by:

$$t_2 = \frac{L\sqrt{1-v^2/c^2}}{c+v} + \frac{L\sqrt{1-v^2/c^2}}{c-v} = \frac{2Lc\sqrt{1-v^2/c^2}}{c^2(1-v^2/c^2)}$$

$$t_2 = \frac{2L}{c} \frac{\sqrt{1-v^2/c^2}}{(\sqrt{1-v^2/c^2})^2} = \frac{2L}{c} \frac{1}{\sqrt{1-v^2/c^2}} = t_1$$

Therefore,  $t_2 - t_1 = 0$  and no fringe shift is expected.